

# Role of Electron Trapping in SRS on NIF Ignition Targets

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D. J. Strozzi: Anomalous 2009; p. 1

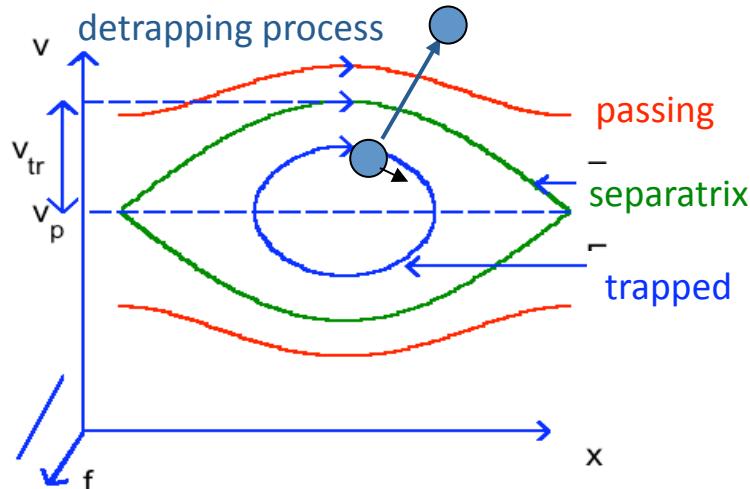
# Summary

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- Electron trapping nonlinearity can either enhance (damping reduction or “kinetic inflation”) or saturate (e.g., frequency shift) SRS.
- Simple assessment of whether trapping is likely provided by “bounce number.”
  - Number of bounce orbits completed before detrapping by collisions or geometric loss.
  - Damping reduction and frequency shift develop smoothly as bounce number increases; no hard threshold.
- Bounce-number assessments of NIF ignition designs show:
  - Trapping is unlikely on the outer beams, where SRS is weak.
  - Trapping may affect SRS on the inner beams, and more so on Be than CH ablatars.

# Likelihood of electron trapping nonlinearity quantified by “bounce number” $N_B$

- Electron trapping nonlinearities (e.g., inflation, frequency shift, Langmuir-wave self-focusing) are effective only if the electrons resonant w/ plasma wave complete  $\sim 1$  bounce orbit before being detrapped.



## Important detrapping processes:

1. Speckle sideloss (geometric effect):  $N_{B,sl}$
2. Collisions: electron-electron and electron-ion treated together:  $N_{B,coll}$   
(SSD – way too slow to matter)

$$\text{Bounce number: } N_B \equiv \frac{\tau_{de}}{\tau_B} = \frac{\text{detrapping time}}{\text{bounce period}}$$

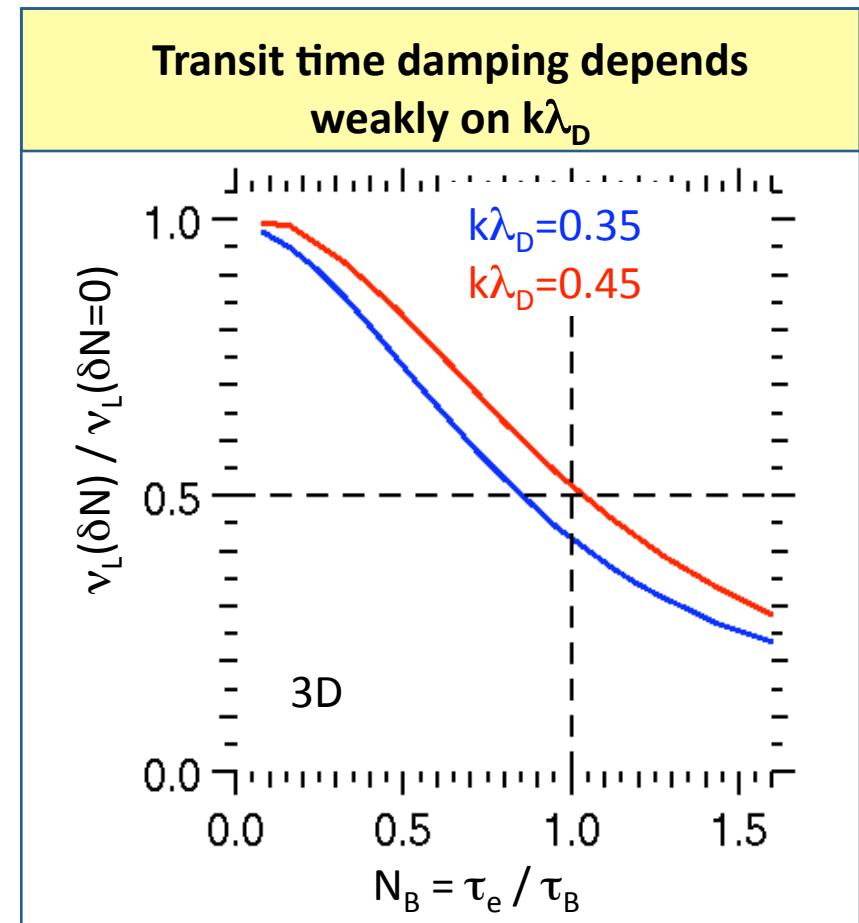
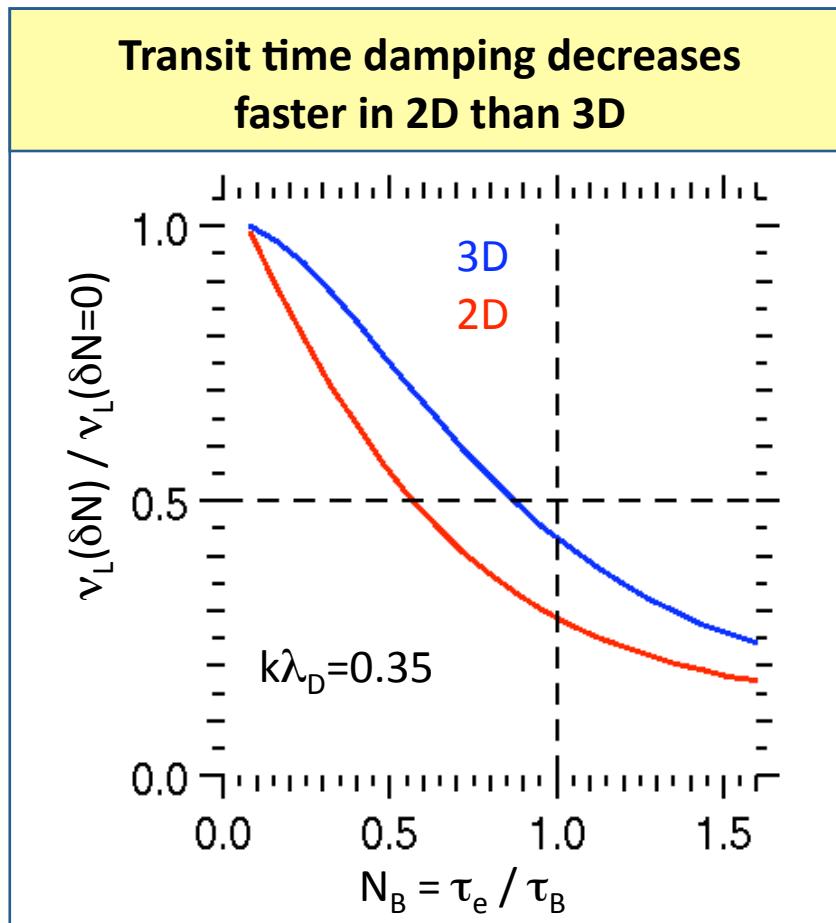
$$\text{Bounce period: } \tau_B \equiv \frac{2\pi}{\omega_{pe}} \sqrt{\frac{n_e}{\delta n}}$$

$$\text{Joint bounce number: } N_B^{-1} = N_{B,sl}^{-1} + N_{B,coll}^{-1} \quad \text{Independent detrapping processes.}$$

$$i^{\text{th}} \text{ process: } N_{B,i} \equiv \frac{\tau_{de,i}}{\tau_B} = \left[ \frac{\delta n}{\delta n_{\text{thresh},i}} \right]^{p_i}$$

**Threshold:**  $\delta n = \delta n_{\text{thresh},i} \rightarrow N_{B,i} = 1$

## Rose calculation of nonlinear transit-time damping in finite speckle give $N_B \approx 1$ for significant damping reduction



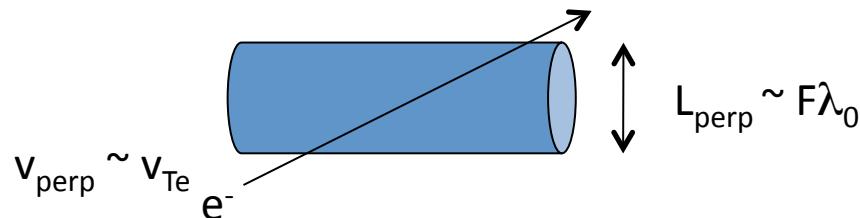
$$\frac{v_L(\phi)}{v_L(\phi = 0)} \approx G \left( \frac{\omega_b}{v_{\text{side loss}}} \right)$$

$v_{\text{side loss}} \sim v_e / (\text{Langmuir wave scale length})$

\*With reduced damping a given high-frequency beat ponderomotive force drives a larger Langmuir wave, so  $N_B$  from the linear  $\delta n$  is an under-estimate.

## Sideloss threshold: lower in 2D than 3D

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$$N_{B,sl} = \frac{\tau_{sl}}{\tau_B} = K_{sl} \frac{L_\perp}{v_{T_e} \tau_B} = \left[ \frac{\delta n}{\delta n_{sl}} \right]^{1/2}$$

$K_{sl} = (0.98, 0.48)$  in (2D, 3D)  
(thermal Maxwellian leaving cylinder)

### Speckle sideloss:

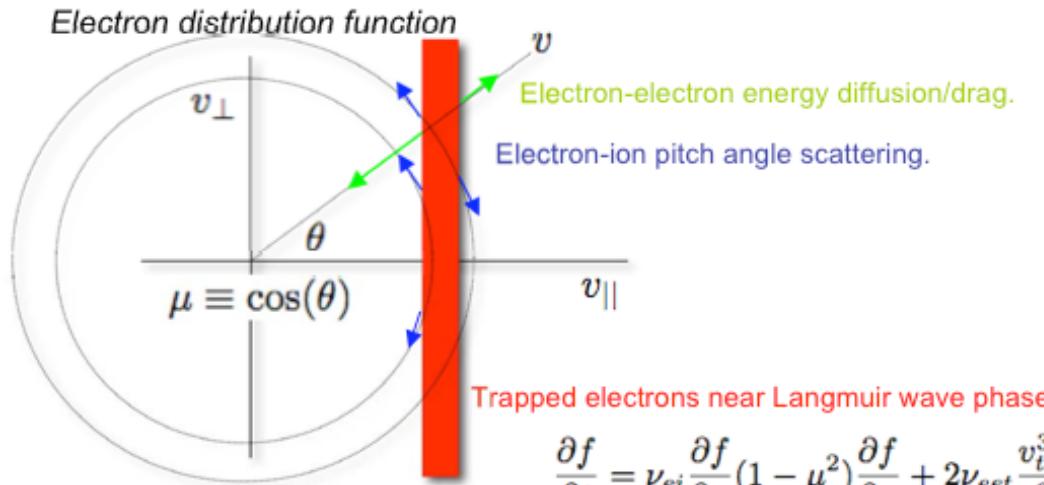
$$L_\perp \approx F\lambda_0 \quad \frac{\delta n_{sl}}{n_e} \equiv 1.33 \cdot 10^{-4} \left[ \frac{8}{F} \right]^2 \frac{n_c}{n_e} T_{e,kV} \quad [\text{3D}]$$

Endloss also occurs,  
usually much slower:

$$\tau_{el} \sim \frac{L_\parallel}{v_{\text{phase}}} \quad L_\parallel \sim 5F^2\lambda_0 \quad \frac{\tau_{sl}}{\tau_{el}} \sim \frac{1}{5F} \frac{v_{\text{phase}}}{v_{T_e}} \ll 1$$

<sup>1</sup>E. A. Williams, D. J. Strozzi, et al., Anomalous Absorption Meeting, 2008.

# Collisional thresholds: e-e and e-i treated together



$$\frac{\partial f}{\partial t} = \nu_{ei} \frac{\partial f}{\partial \mu} (1 - \mu^2) \frac{\partial f}{\partial \mu} + 2\nu_{eet} \frac{v_t^3}{v^2} \frac{\partial}{\partial v} \left( f + \frac{v_t^2}{v} \frac{\partial f}{\partial v} \right)$$

$$N_{B,coll} = \frac{\tau_{coll}}{\tau_B} = \left[ \frac{\delta n}{\delta n_{coll}} \right]^{3/2} \quad \frac{\delta n_{coll}}{n_e} \equiv \left[ 2\pi \ln 2 \frac{\nu_{ei}(v = v_T)}{\omega_p} \frac{(k\lambda_D)^2}{G[v_{ph}/v_{Te}, Z_{eff}]} \right]^{2/3}$$

For  $v_p \gg v_{Te}$ :

$$\tau_{coll} \approx \frac{28.4}{3 + Z_{eff}} \frac{n_e \lambda_{De}^3}{\ln \Lambda} \frac{(\omega/\omega_{pe})^3}{(k\lambda_{De})^5} \frac{\delta n}{n_e} + O\left(\frac{v_p}{v_{Te}}\right)^2$$

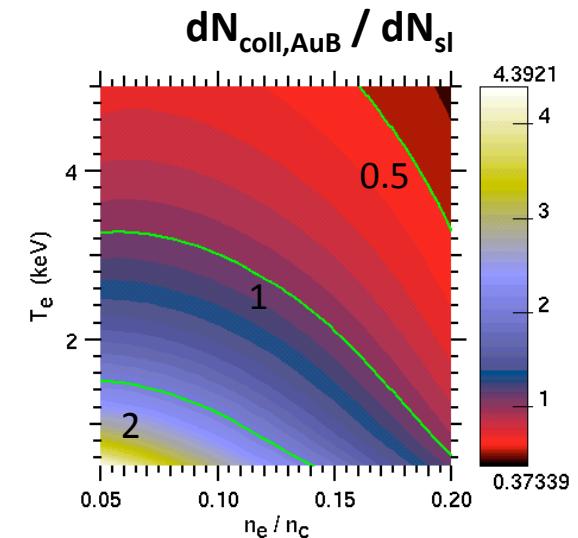
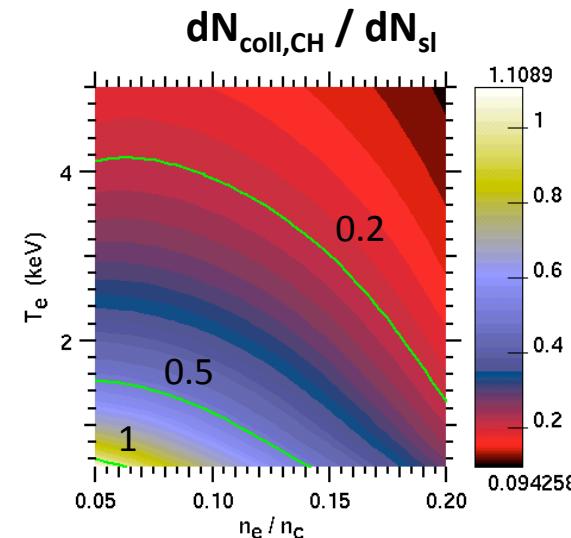
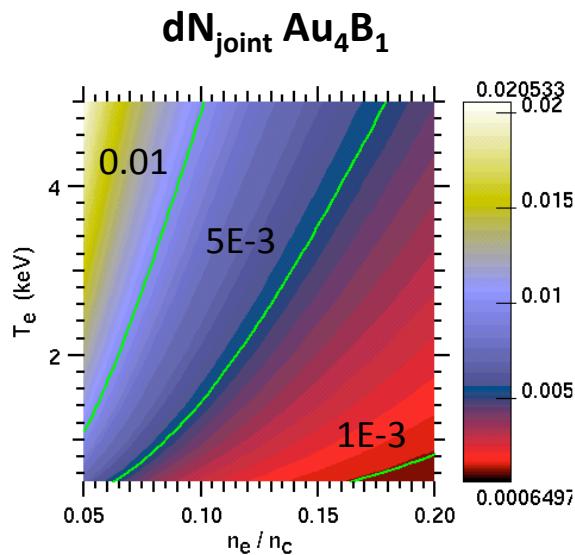
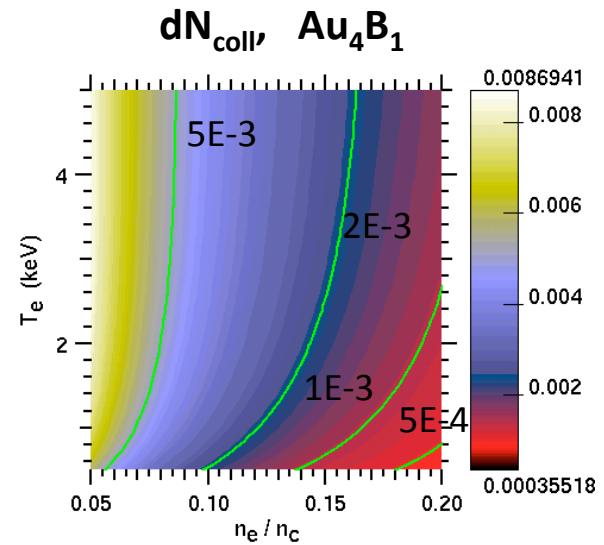
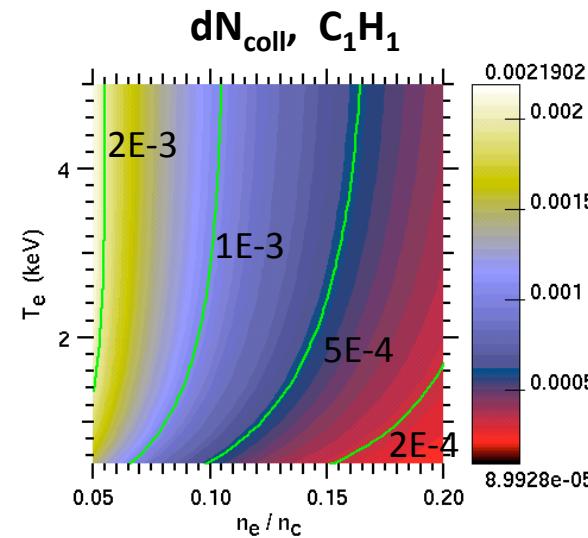
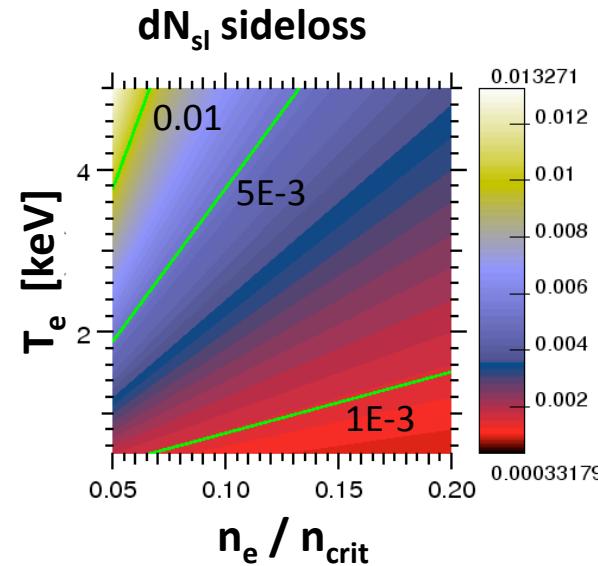
Depends on wave amplitude  $\delta n$ , unlike sideloss

3 (e-e energy diffusion/drag + pitch angle)  
+  $Z_{eff}$  (e-ion pitch angle)

<sup>1</sup>E. A. Williams, D. J. Strozzi, et al., Anomalous Absorption Meeting, 2008.

Trapping threshold for sideloss usually dominates collision threshold, but collisions can matter for high-Z, cold, low-density plasmas

$$dN = dn/n_e$$



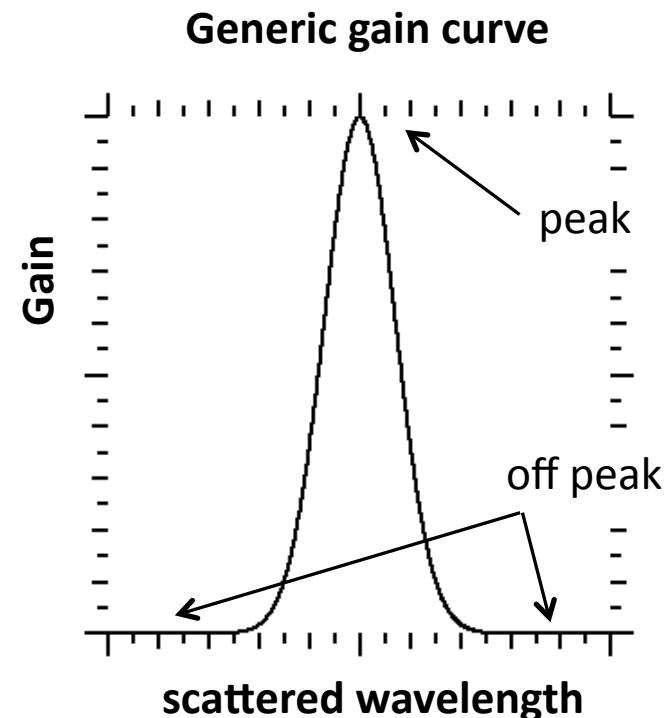
# Overview of trapping risk for NIF designs

trapping  
more  
likely

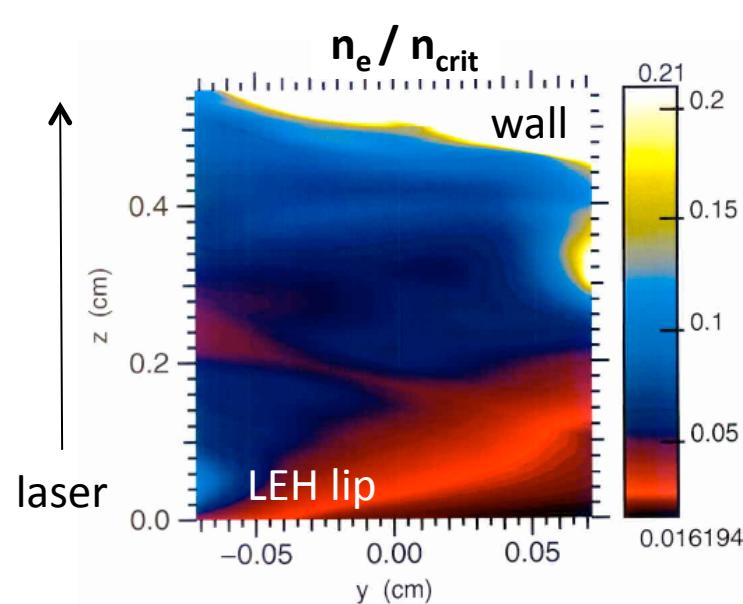
- outer beam, off peak: Pierre Michel looked w/ SLIP closer to LEH than max gain (higher  $T_e$ , lower  $n_e$ , higher  $k\lambda_{De}$ ); even less risk than on-resonance.
- outer beam, peak: SRS is linearly weak, stays below trapping threshold; nonlinearity not a concern.
- inner beam, off peak: assessed with ray-based DEPLET code.
- inner beam, peak: Trapping may occur here, but does it inflate or saturate?

\* **"Peak" SRS:** at scattered wavelength of max gain; we generally envelope around this in pf3d. Assessed by post-processing the Langmuir waves driven in pf3d.

\* **"Off peak" SRS:** at wavelengths with lower linear gain; less SRS expected, but a pf3d run won't include it unless we envelope around an off-peak wavelength.

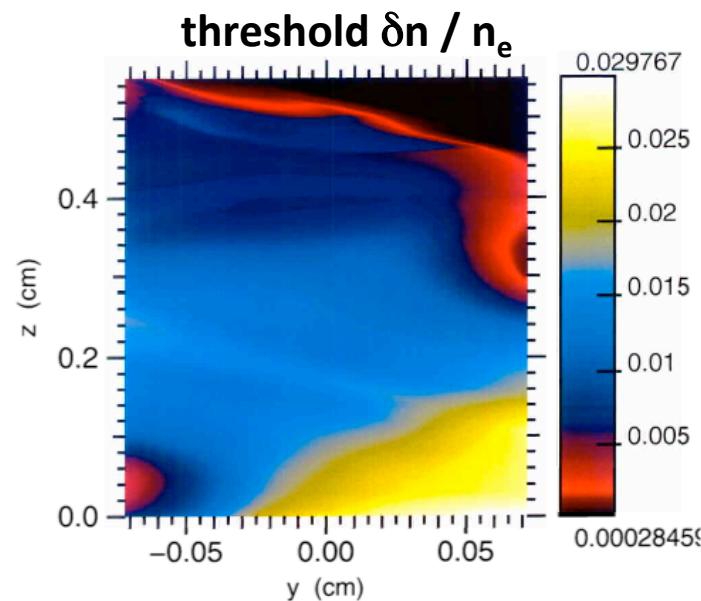
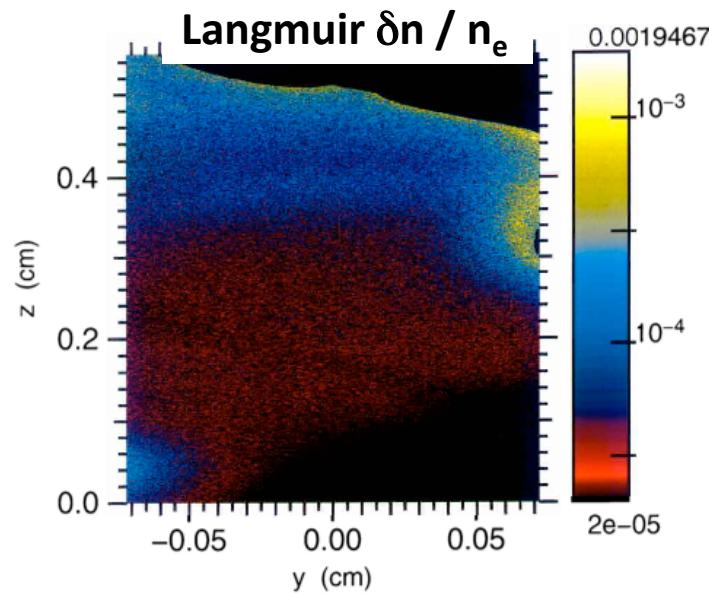


**Outer beam peak SRS: pf3d run of 50 deg. beam,  $T_{\text{rad}} = 285$  eV,  
Be ablator, at 12 ns (peak power)**

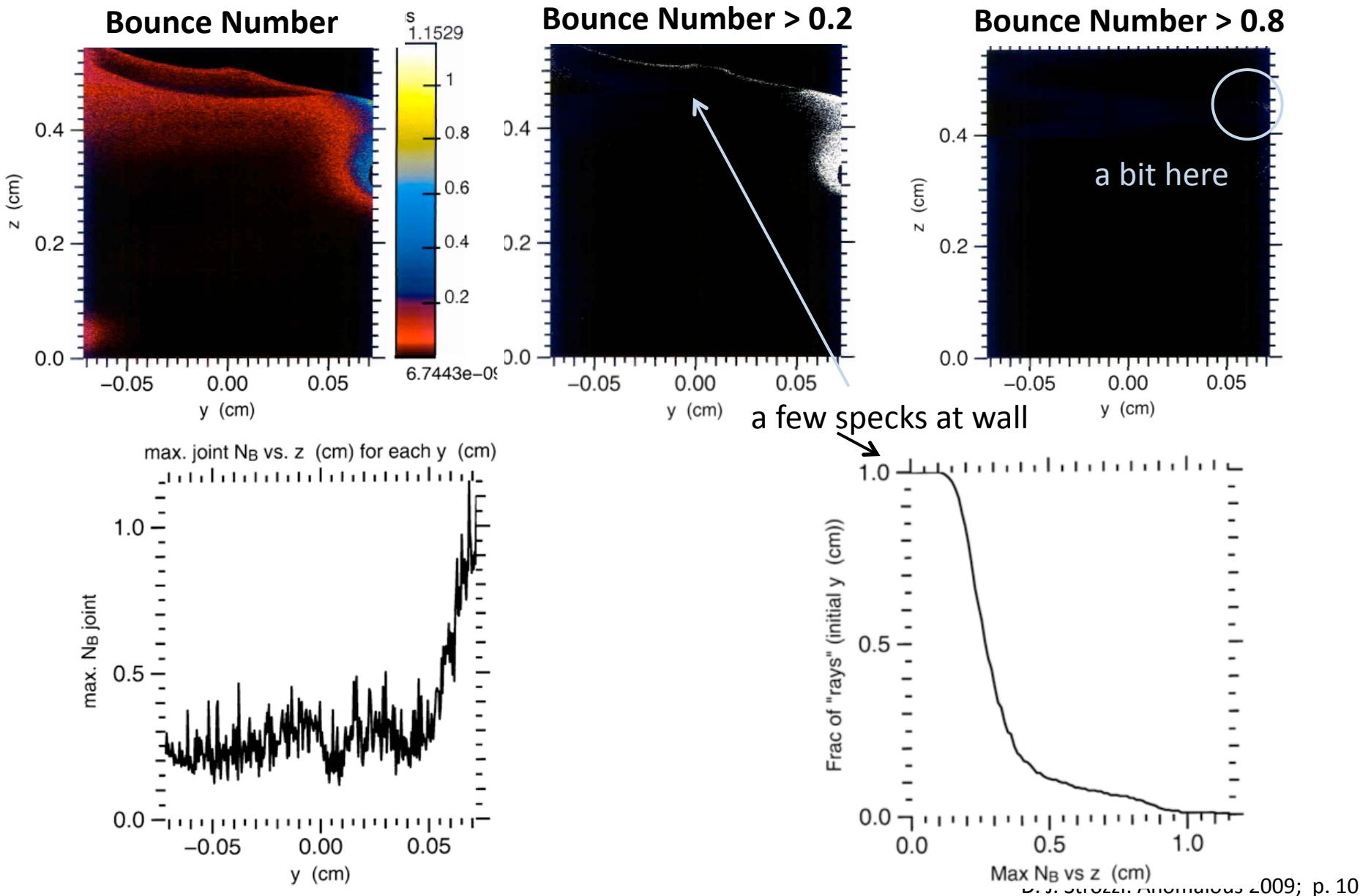


**pf3d SRS reflectivity  $\sim 10^{-6}$**

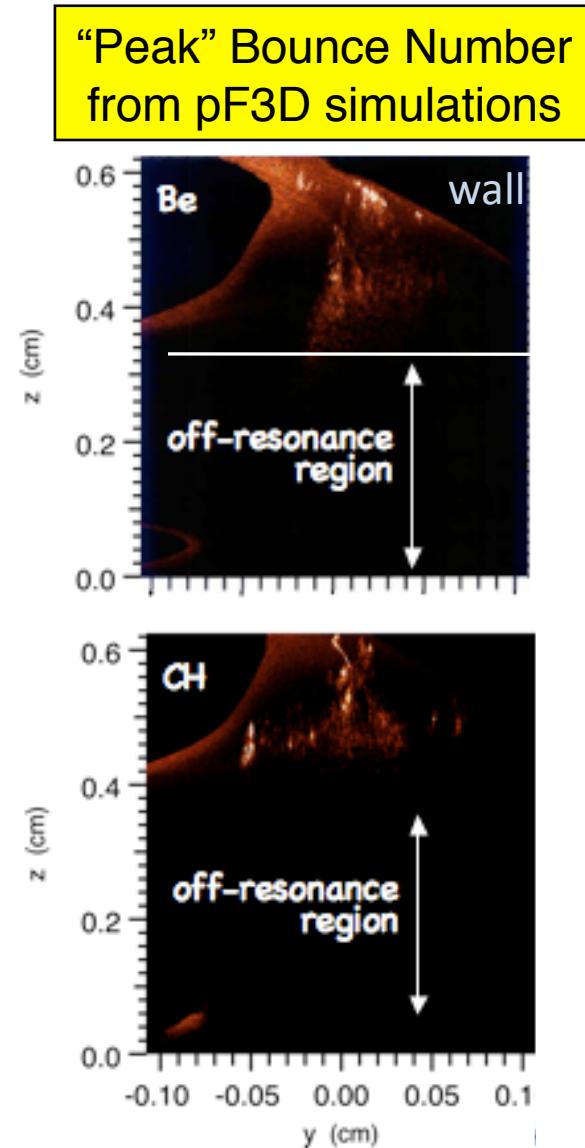
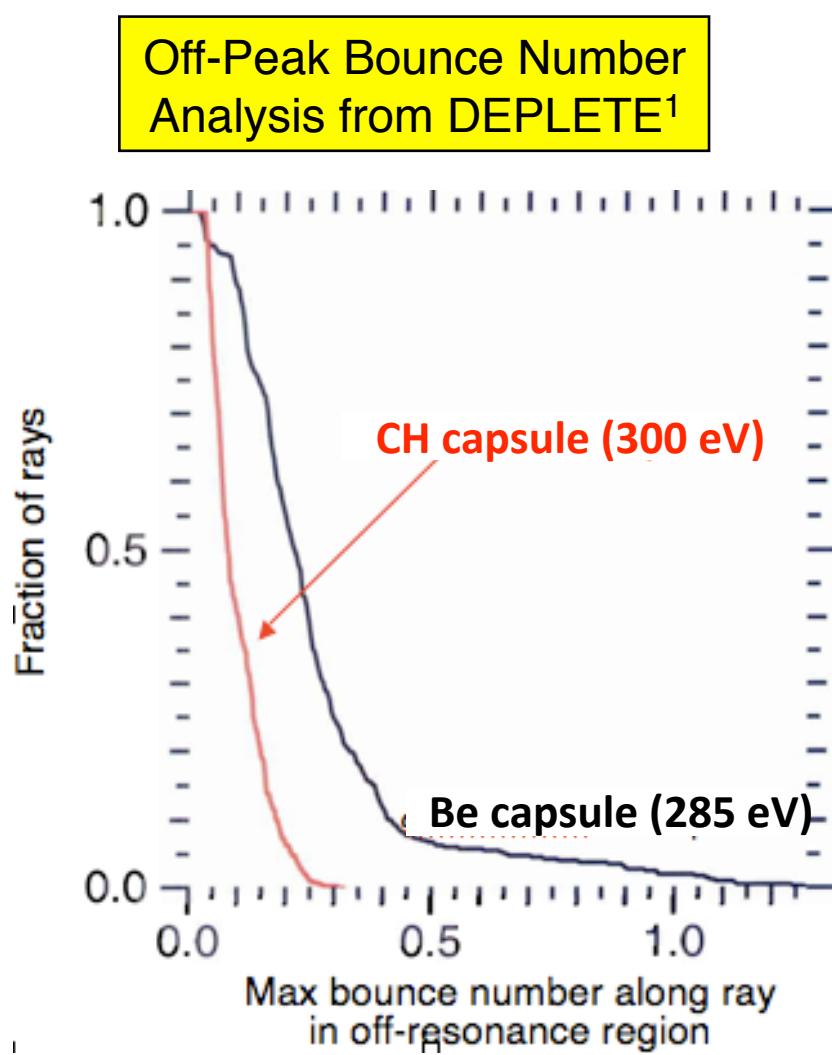
Off-peak outer beam:  
Examined by Pierre Michel w/  
SLIP, trapping even less of a  
concern.



## Outer beam peak SRS: bounce number << 0.5 almost everywhere: trapping is not a concern (same results for CH design)

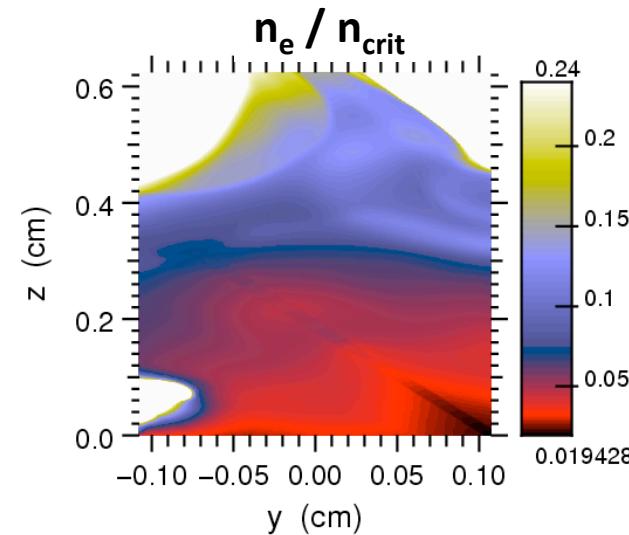
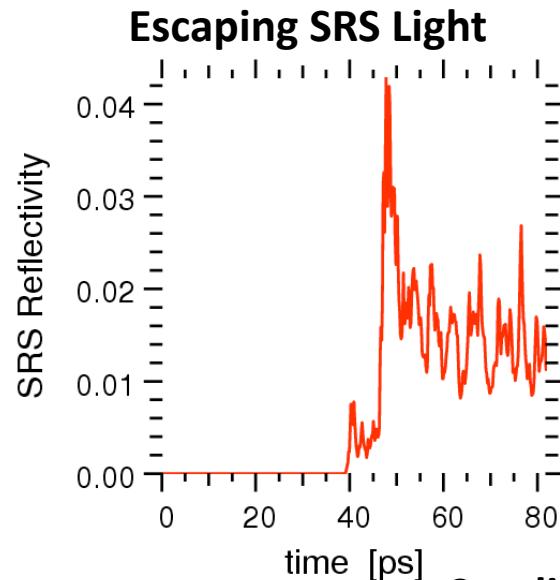


# Off peak inner beam SRS: bounce number assessment shows little risk for kinetic inflation

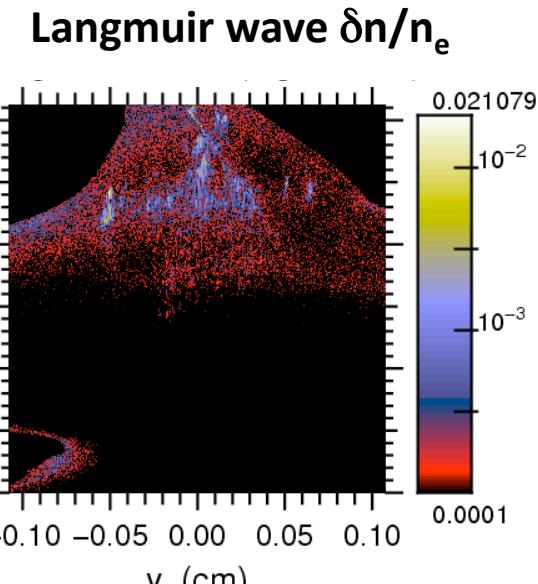
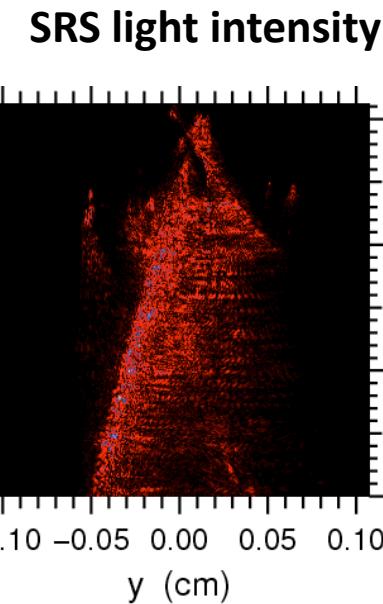
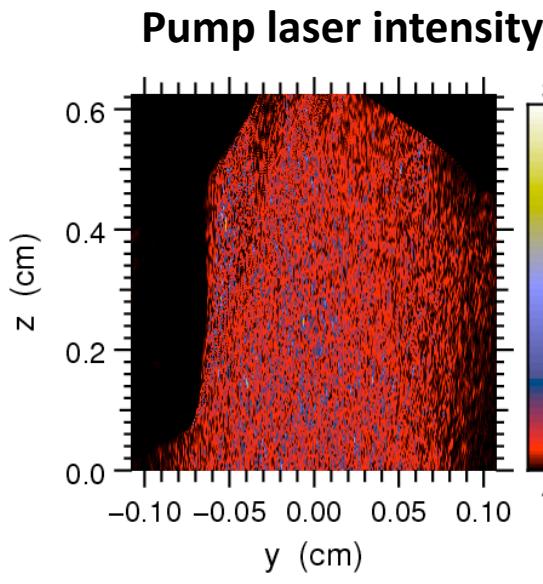


<sup>1</sup>D. J. Strozzi *et al.*, Phys. Plasmas 15, 102703 (2008)

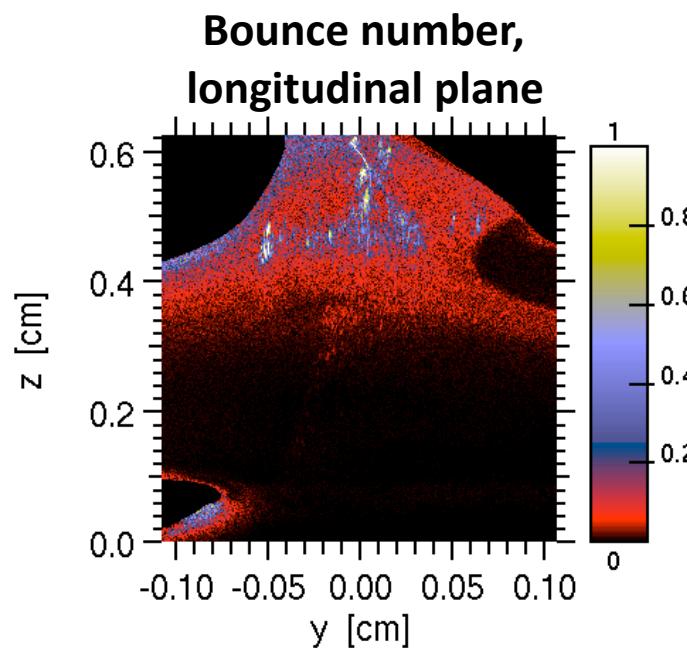
# Inner beam peak SRS: post-process pF3D run of CH ablator, 300 eV radiation temperature, LEH liner



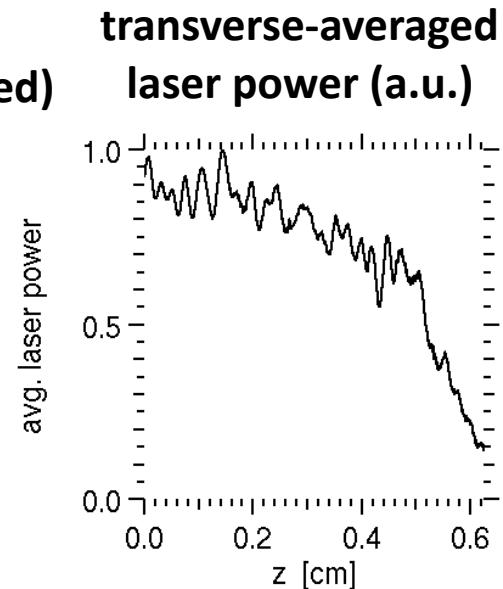
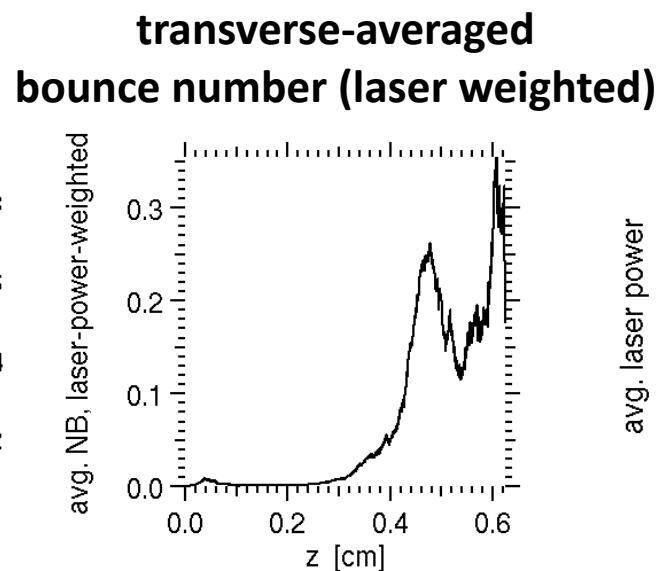
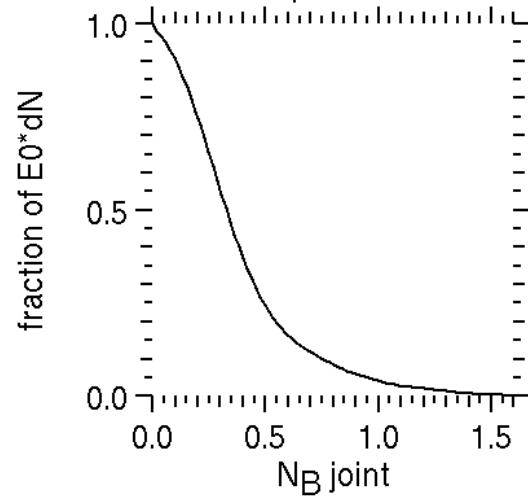
Conditions on longitudinal (yz) plane, 82 ps



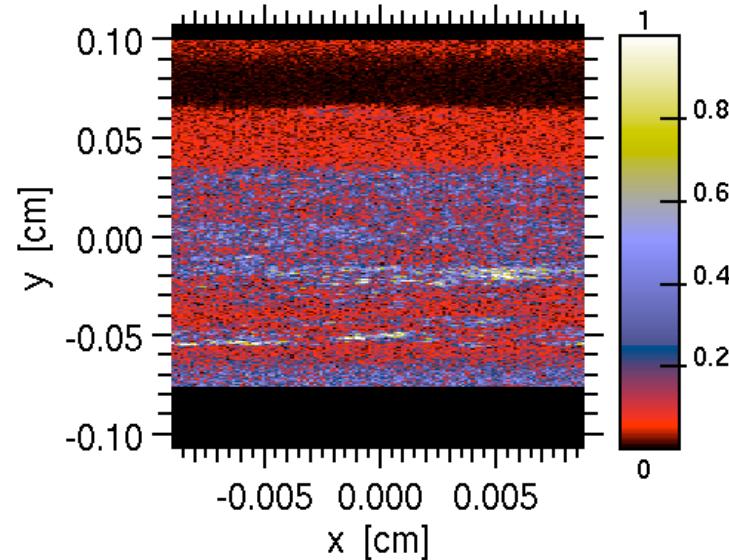
# CH ablator case: conditions at run end (82.4 ps)



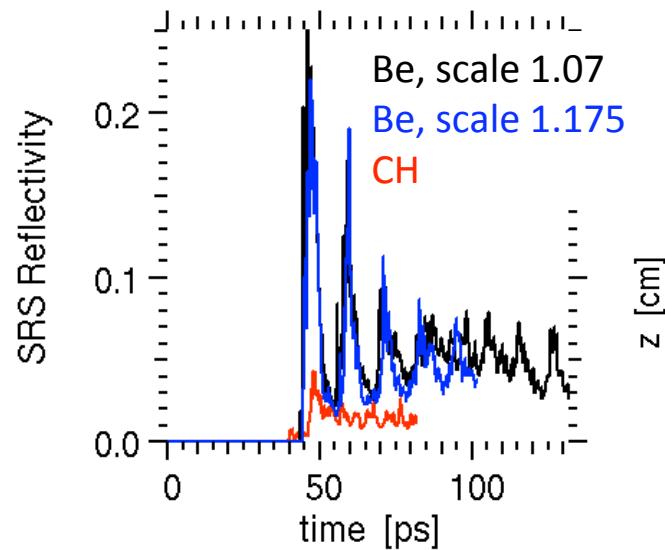
Fraction of scattered coupling ( $E_{\text{las}} \cdot \delta n^*$ )  
above a bounce number,  $z = 0.47 \text{ cm}$



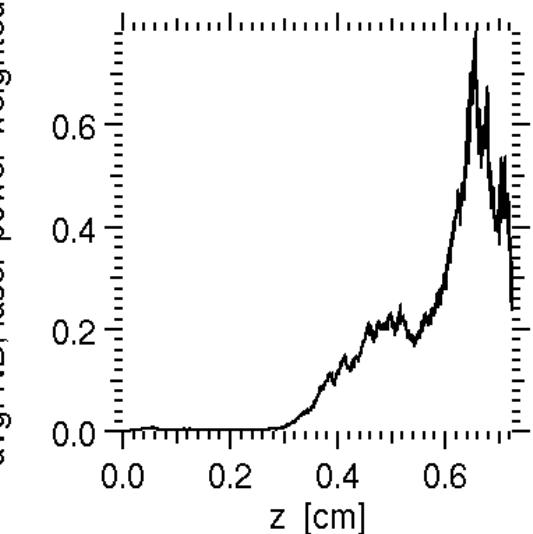
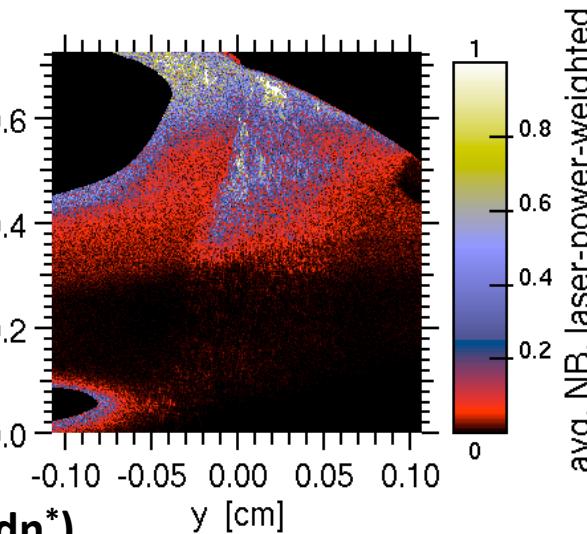
Bounce number at  $z = 0.47 \text{ cm}$



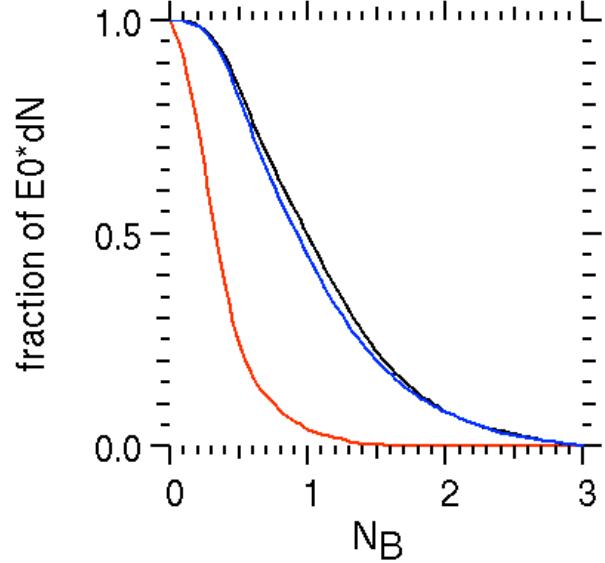
# Comparison of CH and Be ablators: more SRS, and more trapping risk, in Be



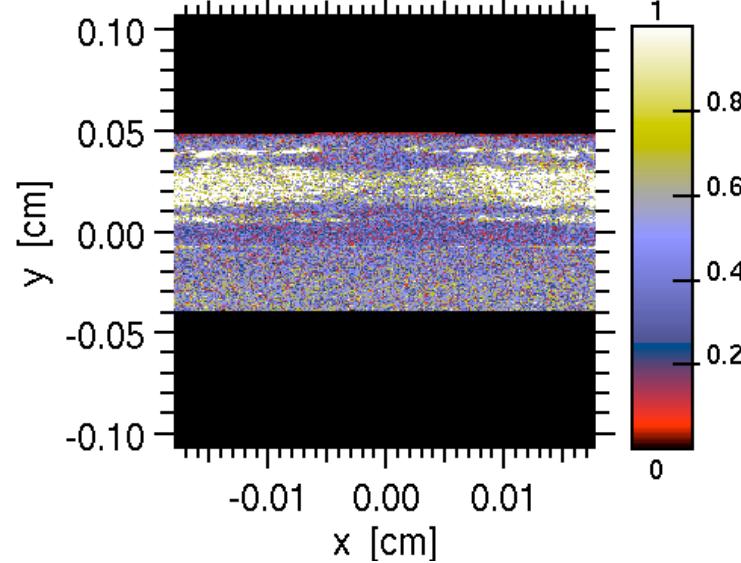
Bounce number Be scale 1.07, time = 101 ps



Fraction of scattered coupling ( $E_{0^*}dn^*$ )  
above a bounce number, over xy plane



Bounce number at z = 63 cm



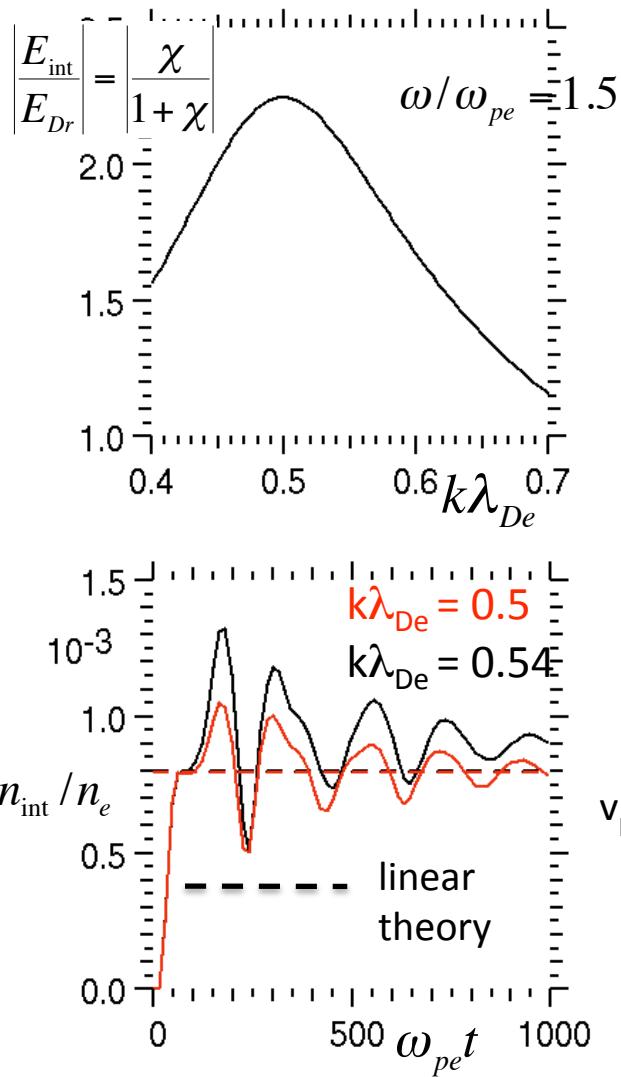
## Summary and Future Work

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- “Bounce number” provides a simple assessment of whether electron trapping nonlinearity can overcome detrapping processes (sideloss, collisions).
  - Sideloss is usually the dominant detrapping process.
- SRS on NIF outer beams seems below trapping threshold.
- SRS on NIF inner beams are more worrisome; designs with CH ablators less so than Be.
- A reduced model is needed to quantitatively study trapping effects: does it enhance SRS (inflation) or saturate it?
- Work is underway to implement such a model in pF3D, and benchmark it against kinetic simulations (R. Berger, H. Rose, D. Strozzi).

# 1D Vlasov simulations with Sapristi<sup>1</sup> of driven EPW's in LEH conditions: departures from linear theory, even though $N_B \gg 1$

“Resonance” is broad, not that high



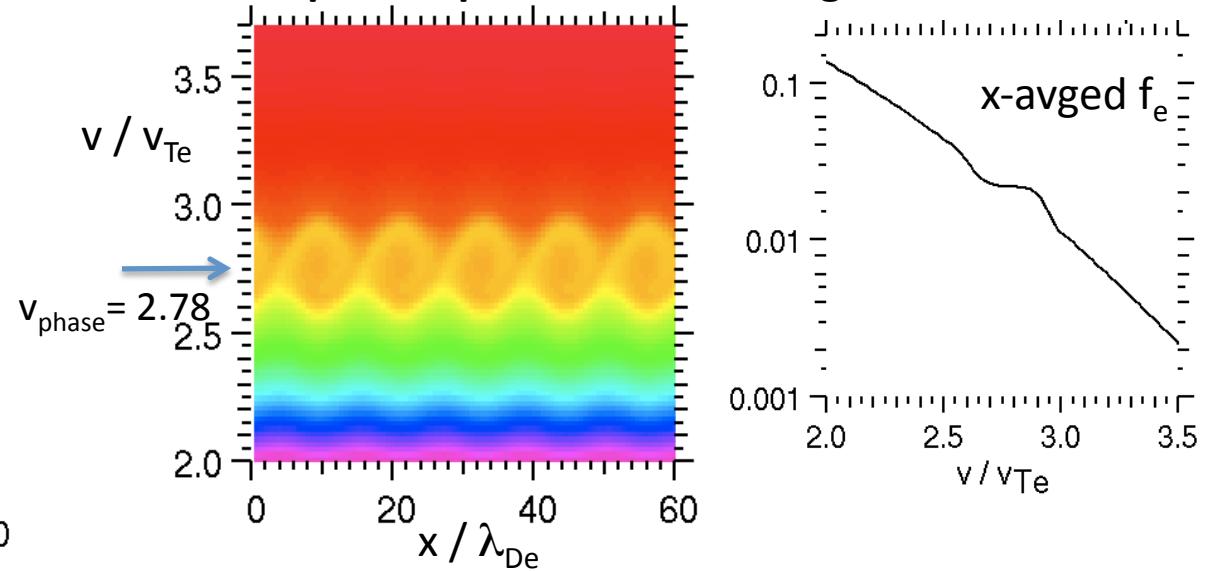
Homogenous, periodic plasma:

$$n_e/n_{\text{crit}} = 0.07 \quad T_e = 5 \text{ keV}; \\ v_{\text{Krook}} = 4.3 \times 10^{-4} \omega_{pe} \quad (\text{sideloss for } L_{\text{perp}} = 100 \text{ um})$$

$$\text{Krook relaxation: } \partial_t f|_{\text{Krook}} = v_K \cdot (n\hat{f}_0 - f)$$

$$\text{Bounce number in linear field } \gg 1 \quad N_B = \frac{\omega_B}{2\pi v_K} = 14.3$$

**Distribution for  $k\lambda_{\text{De}} = 0.54$ ,  $t \omega_{pe} = 750$ :**  
**phase-space vortices; x-avgd  $f$  flattened**



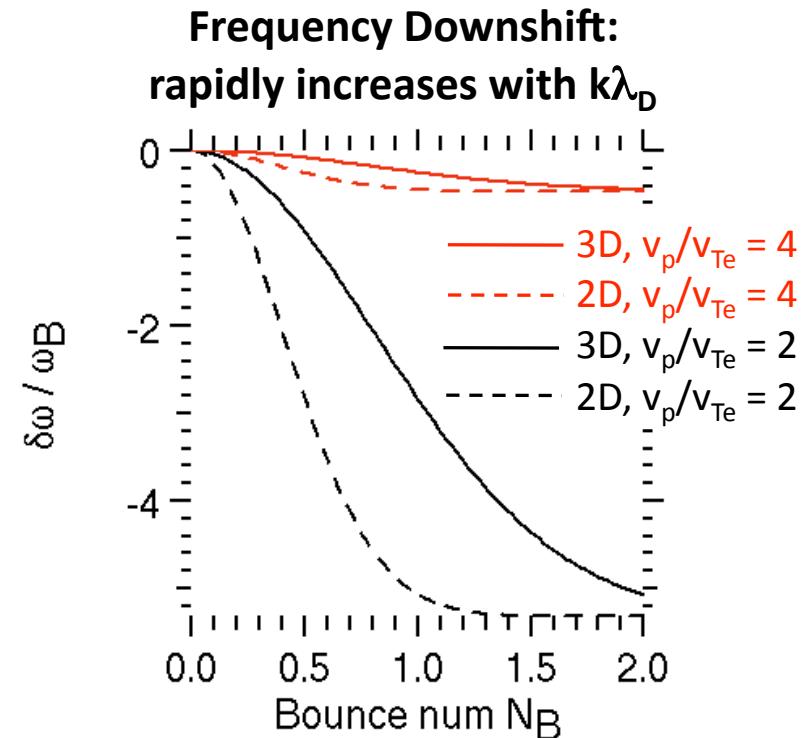
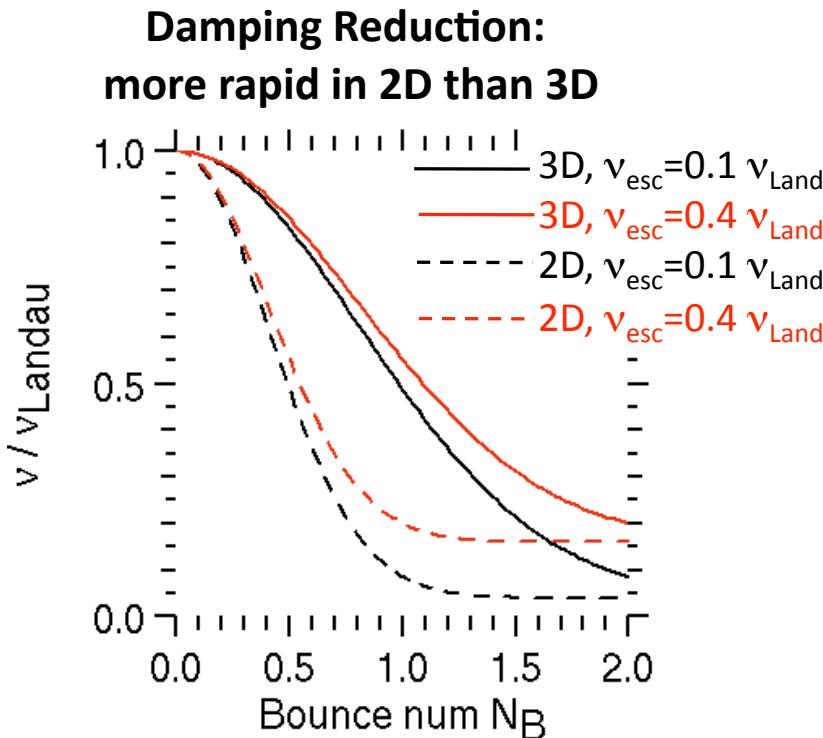
<sup>1</sup> S. Brunner, E. J. Valeo, PRL 93, 145003 (2004).

## Reduced model by H. Rose, for Langmuir waves of finite transverse size

damping reduction:  $\frac{v}{v_{\text{Landau}}} = f + 0.4(1-f)\frac{v_{\text{esc}}}{v_{\text{Landau}}}$        $f = \exp\left[-\ln 2 \cdot \left(\frac{2\pi}{3(D-1)}\right)^2 N_B^2\right]$       D = dimensionality = 2,3

frequency shift:  $\frac{\delta\omega}{\omega_B} = -0.88\left(\frac{v_p}{v_{Te}}\right)^3 f_{mxw}''(v_p/v_{Te}) \cdot (1-f)$        $\frac{v_{\text{esc}}}{v_{\text{Landau}}} \sim \frac{v_{Te}}{L_\perp}$       Depends on  $k\lambda_D$ , 2D/3D

Benchmarked by transit-time damping and PIC calculations.



# DEPLET<sup>1</sup> performs ray-based, steady-state backscatter calculations

Pump:	$\frac{d}{dz} I_0(z) = -\kappa_0 I_0 - I_0 \int d\omega_1 \frac{\omega_0}{\omega_1} (\tau_1 + \Gamma_1 i_1)$			
Scattered Light:	$\frac{\partial}{\partial z} i_1(z, \omega_1) = \kappa_1 i_1 - \Sigma_1 - I_0 (\tau_1 + \Gamma_1 i_1)$			
	inv. brems. damping	brems. source	Thomson scattering	SBS/SRS coupling

The code DEPLET does:

- use 1-D plasma conditions from 3-D ray-trace
- handle a spectrum of scattered frequencies
- use a strong damping limit plasma-wave
- deplete the laser pump
- use Thomson scatter/bremsstrahlung noise sources
- inverse-bremsstrahlung light wave damping
- use linear kinetic coupling coefficients
- include collisional damping of Langmuir waves
- model whole-beam focusing

The code DEPLET does not:

- include temporal effects
- include laser speckle effects
- include multi-D effects

<sup>1</sup>D. J. Strozzi, E. A. Williams, D. E. Hinkel, D. H. Froula, R. A. London, D. A. Callahan, Phys. Plasmas 15, 102703 (2008).